

# Package: cicalc (via r-universe)

May 8, 2026

**Type** Package

**Title** Calculate Confidence Intervals

**Version** 0.2.1

**Description** This calculates a variety of different CIs for proportions and difference of proportions that are commonly used in the pharmaceutical industry including Wald, Wilson, Clopper-Pearson, Agresti-Coull and Jeffreys for proportions. And Miettinen-Nurminen (1985) <[doi:10.1002/sim.4780040211](https://doi.org/10.1002/sim.4780040211)>, Wald, Haldane, and Mee <[https://www.lexjansen.com/wuss/2016/127\\_Final\\_Paper\\_PDF.pdf](https://www.lexjansen.com/wuss/2016/127_Final_Paper_PDF.pdf)> for difference in proportions.

**License** Apache License (>= 2)

**URL** <https://gsk-biostatistics.github.io/cicalc/>,  
<https://github.com/gsk-biostatistics/cicalc>

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ci\_prop\_agresti\_coull *Agresti-Coull CI*

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### Description

Calculates the Agresti-Coull interval (created by Alan Agresti and Brent Coull) by (for 95% CI) adding two successes and two failures to the data and then using the Wald formula to construct a CI.

### Usage

```
ci_prop_agresti_coull(x, conf.level = 0.95, data = NULL)
```

### Arguments

x	(binary/numeric/logical) vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)
conf.level	(scalar numeric) a scalar in (0,1) indicating the confidence level. Default is 0.95
data	(data.frame) Optional data frame containing the variables specified in x and by.

**Details**

$$\left( \frac{\tilde{p} + z_{\alpha/2}^2/2}{n + z_{\alpha/2}^2} \pm z_{\alpha/2} \sqrt{\frac{\tilde{p}(1 - \tilde{p})}{n} + \frac{z_{\alpha/2}^2}{4n^2}} \right)$$

**Value**

An object containing the following components:

n	Number of responses
N	Total number
estimate	The point estimate of the proportion
conf.low	Lower bound of the confidence interval
conf.high	Upper bound of the confidence interval
conf.level	The confidence level used
method	Type of method used

---

ci\_prop\_clopper\_pearson

*Clopper-Pearson CI*

---

**Description**

Calculates the Clopper-Pearson interval by calling `stats::binom.test()`. Also referred to as the exact method.

**Usage**

```
ci_prop_clopper_pearson(x, conf.level = 0.95, data = NULL)
```

**Arguments**

x	(binary/numeric/logical) vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)
conf.level	(scalar numeric) a scalar in (0,1) indicating the confidence level. Default is 0.95
data	(data.frame) Optional data frame containing the variables specified in x and by.

**Details**

$$\left( 1 + \frac{N - n + 1}{nF[\frac{\alpha}{2}; 2n, 2(N - n + 1)]} \right)^{-1}, \left( 1 + \frac{N - n}{(n + 1)F[1 - \frac{\alpha}{2}; 2(n + 1), 2(N - n)]} \right)^{-1}$$

**Value**

An object containing the following components:

n	Number of responses
N	Total number
estimate	The point estimate of the proportion
conf.low	Lower bound of the confidence interval
conf.high	Upper bound of the confidence interval
conf.level	The confidence level used
method	Type of method used

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ci_prop_diff_ha	<i>Anderson-Hauck Confidence Interval for Difference in Proportions</i>
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**Description**

Anderson-Hauck Confidence Interval for Difference in Proportions

**Usage**

```
ci_prop_diff_ha(x, by, conf.level = 0.95, data = NULL)
```

**Arguments**

x	(binary/numeric/logical) vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)
by	(string) A character or factor vector with exactly two unique levels identifying the two groups to compare. Can also be a column name if a data frame provided in the data argument.
conf.level	(scalar numeric) a scalar in (0,1) indicating the confidence level. Default is 0.95
data	(data.frame) Optional data frame containing the variables specified in x and by.

**Details**

The confidence interval is given by:

$$(\hat{p}_1 - \hat{p}_2) \pm \left[ \frac{1}{2 \min(n_1, n_2)} + z \sqrt{\frac{\hat{p}_1(1 - \hat{p}_1)}{n_1 - 1} + \frac{\hat{p}_2(1 - \hat{p}_2)}{n_2 - 1}} \right]$$

**Value**

An object containing the following components:

n	The number of responses for each group
N	The total number in each group
estimate	The point estimate of the difference in proportions
conf.low	Lower bound of the confidence interval
conf.high	Upper bound of the confidence interval
conf.level	The confidence level used
method	Anderson-Hauck Confidence Interval

**References**

Hauck WW, Anderson S. (1986) A comparison of large-sample confidence interval methods for the difference of two binomial probabilities *The American Statistician* 40(4). p.318-322. [Constructing Confidence Intervals for the Differences of Binomial Proportions in SAS](#)

**Examples**

```
responses <- expand(c(9, 3), c(10, 10))
arm <- rep(c("treat", "control"), times = c(10, 10))

# Calculate 95% confidence interval for difference in proportions
ci_prop_diff_ha(x = responses, by = arm)
```

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ci\_prop\_diff\_haldane *Haldane Confidence Interval for Difference in Proportions*

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**Description**

Haldane Confidence Interval for Difference in Proportions

**Usage**

```
ci_prop_diff_haldane(x, by, conf.level = 0.95, data = NULL)
```

**Arguments**

x	(binary/numeric/logical) vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)
by	(string) A character or factor vector with exactly two unique levels identifying the two groups to compare. Can also be a column name if a data frame provided in the data argument.
conf.level	(scalar numeric) a scalar in (0,1) indicating the confidence level. Default is 0.95
data	(data.frame) Optional data frame containing the variables specified in x and by.

**Details**

The confidence interval is calculated by  $\theta^* \pm w$  where:

$$\theta^* = \frac{(\hat{p}_1 - \hat{p}_2) + z^2 v (1 - 2\hat{\psi})}{1 + z^2 u}$$

where

$$w = \frac{z}{1 + z^2 u} \sqrt{u\{4\hat{\psi}(1 - \hat{\psi}) - (\hat{p}_1 - \hat{p}_2)^2\} + 2v(1 - 2\hat{\psi})(\hat{p}_1 - \hat{p}_2) + 4z^2 v^2 (1 - 2\hat{\psi})^2}$$

$$\hat{\psi} = \frac{\hat{p}_1 + \hat{p}_2}{2}$$

$$u = \frac{1/n_1 + 1/n_2}{4}$$

$$v = \frac{1/n_1 - 1/n_2}{4}$$

**Value**

An object containing the following components:

n	The number of responses for each group
N	The total number in each group
estimate	The point estimate of the difference in proportions (theta*)
conf.low	Lower bound of the confidence interval
conf.high	Upper bound of the confidence interval
conf.level	The confidence level used
method	Haldane Confidence Interval

**References**

[Constructing Confidence Intervals for the Differences of Binomial Proportions in SAS](#)

**Examples**

```
responses <- expand(c(9, 3), c(10, 10))
arm <- rep(c("treat", "control"), times = c(10, 10))

# Calculate 95% confidence interval for difference in proportions
ci_prop_diff_haldane(x = responses, by = arm)
```

ci\_prop\_diff\_jp

*Jeffreys-Perks Confidence Interval for Difference in Proportions***Description**

Jeffreys-Perks Confidence Interval for Difference in Proportions

**Usage**

ci\_prop\_diff\_jp(x, by, conf.level = 0.95, data = NULL)

**Arguments**

**x** (binary/numeric/logical)  
vector of a binary values, i.e. a logical vector, or numeric with values  $c(0, 1)$

**by** (string)  
A character or factor vector with exactly two unique levels identifying the two groups to compare. Can also be a column name if a data frame provided in the data argument.

**conf.level** (scalar numeric)  
a scalar in (0,1) indicating the confidence level. Default is 0.95

**data** (data.frame)  
Optional data frame containing the variables specified in x and by.

**Details**The confidence interval is calculated by  $\theta^* \pm w$  where:

$$\theta^* = \frac{(\hat{p}_1 - \hat{p}_2) + z^2 v (1 - 2\hat{\psi})}{1 + z^2 u}$$

where

$$w = \frac{z}{1 + z^2 u} \sqrt{u\{4\hat{\psi}(1 - \hat{\psi}) - (\hat{p}_1 - \hat{p}_2)^2\} + 2v(1 - 2\hat{\psi})(\hat{p}_1 - \hat{p}_2) + 4z^2 v^2 (1 - 2\hat{\psi})^2}$$

$$\hat{\psi} = \frac{1}{2} \left( \frac{x_1 + 1/2}{n_1 + 1} + \frac{x_2 + 1/2}{n_2 + 1} \right)$$

$$u = \frac{1/n_1 + 1/n_2}{4}$$

$$v = \frac{1/n_1 - 1/n_2}{4}$$

**Value**

An object containing the following components:

n	The number of responses for each group
N	The total number in each group
estimate	The point estimate of the difference in proportions (theta*)
conf.low	Lower bound of the confidence interval
conf.high	Upper bound of the confidence interval
conf.level	The confidence level used
method	Jeffreys-Perks Confidence Interval

**References**

[Constructing Confidence Intervals for the Differences of Binomial Proportions in SAS](#)

**Examples**

```
responses <- expand(c(9, 3), c(10, 10))
arm <- rep(c("treat", "control"), times = c(10, 10))

# Calculate 95% confidence interval for difference in proportions
ci_prop_diff_jp(x = responses, by = arm)
```

---

ci\_prop\_diff\_mee      *Mee Confidence Interval for Difference in Proportions*

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**Description**

Mee Confidence Interval for Difference in Proportions

**Usage**

```
ci_prop_diff_mee(x, by, conf.level = 0.95, delta = NULL, data = NULL)
```

**Arguments**

x	(binary/numeric/logical) vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)
by	(string) A character or factor vector with exactly two unique levels identifying the two groups to compare. Can also be a column name if a data frame provided in the data argument.
conf.level	(scalar numeric) a scalar in (0,1) indicating the confidence level. Default is 0.95

delta	(numeric) Optionally a single number or a vector of numbers between -1 and 1 (not inclusive) to set the difference between two groups under the null hypothesis. If provided, the function returns the test statistic and p-value under the delta hypothesis.
data	(data.frame) Optional data frame containing the variables specified in x and by.

### Details

The confidence interval is calculated by  $\theta^* \pm w$  where:

$$\theta^* = \frac{(\hat{p}_1 - \hat{p}_2) + z^2 v (1 - 2\hat{\psi})}{1 + z^2 u}$$

where

$$w = \frac{z}{1 + z^2 u} \sqrt{u\{4\hat{\psi}(1 - \hat{\psi}) - (\hat{p}_1 - \hat{p}_2)^2\} + 2v(1 - 2\hat{\psi})(\hat{p}_1 - \hat{p}_2) + 4z^2 v^2 (1 - 2\hat{\psi})^2}$$

$$\hat{\psi} = \frac{1}{2} \left( \frac{x_1 + 1/2}{n_1 + 1} + \frac{x_2 + 1/2}{n_2 + 1} \right)$$

$$u = \frac{1/n_1 + 1/n_2}{4}$$

$$v = \frac{1/n_1 - 1/n_2}{4}$$

### Value

An object containing the following components:

n	The number of responses for each group
N	The total number in each group
estimate	The point estimate of the difference in proportions (p1-p2)
conf.low	Lower bound of the confidence interval
conf.high	Upper bound of the confidence interval
conf.level	The confidence level used
method	Mee Confidence Interval

### References

[Constructing Confidence Intervals for the Differences of Binomial Proportions in SAS](#)

### Examples

```
responses <- expand(c(9, 3), c(10, 10))
arm <- rep(c("treat", "control"), times = c(10, 10))

# Calculate 95% confidence interval for difference in proportions
ci_prop_diff_mee(x = responses, by = arm)
```

---

 ci\_prop\_diff\_mh\_strata

*Mantel-Haenszel Common Risk Difference Confidence Interval*


---

### Description

Calculates the confidence interval for the Mantel-Haenszel estimate of the common risk difference across multiple 2x2 tables (strata), using the Sato or Independent Binomial variance estimator.

### Usage

```
ci_prop_diff_mh_strata(
  x,
  by,
  strata,
  conf.level = 0.95,
  sato_var = TRUE,
  data = NULL
)
```

### Arguments

x	(binary/numeric/logical) vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)
by	(string) A character or factor vector with exactly two unique levels identifying the two groups to compare. Can also be a column name if a data frame provided in the data argument.
strata	(numeric) A vector specifying the stratum for each observation. It needs to be the length of x or a multiple of x if multiple levels of strata are present. Can also be a column name (or vector of column names NOT quoted) if a data frame provided in the data argument.
conf.level	(scalar numeric) a scalar in (0,1) indicating the confidence level. Default is 0.95
sato_var	(logical) Use Sato variance estimate
data	(data.frame) Optional data frame containing the variables specified in x and by.

### Details

The Mantel-Haenszel common risk difference is computed as:

$$\hat{\delta}_{MH} = \frac{\sum_k w_k \hat{\delta}_k}{\sum_k w_k}$$

where  $w_k = \frac{n_{xk}n_{yk}}{N_k}$ ,  $\hat{\delta}_k = s_{xk}/n_{xk} - y_{yk}/n_{yk}$ ,  $N_k = n_{xk} + n_{yk}$ ,  $s_{xk}$  and  $s_{yk}$  are the number of events in each group, and  $n_{xk}$ , and  $n_{yk}$  are the group sizes in stratum  $k$ .

The Sato variance is:

$$\hat{\sigma}^2(\hat{\delta}_{MH}) = \frac{\hat{d}_{MH} \sum_k P_k + \sum_k Q_k}{(\sum_k w_k)^2}$$

where  $P_k = \frac{n_{xk}^2 s_{yk} - n_{yk}^2 s_{xk} + n_{xk} n_{yk} (n_{yk} - n_{xk})/2}{N_k^2}$  and  $Q_k = \frac{s_{xk}(n_{yk} - s_{yk}) + s_{yk}(n_{xk} - s_{xk})}{2N_k}$ .

The Cochran Independent Binomial variance is:

$$\hat{\sigma}^2(\hat{\delta}_C) = \sum_k w_k^2 \left[ \frac{\hat{p}_{1k}(1 - \hat{p}_{1k})}{n_{1k}} + \frac{\hat{p}_{2k}(1 - \hat{p}_{2k})}{n_{2k}} \right]$$

where  $\hat{p}_{1k} = \frac{s_{xk}}{n_{xk}}$  and  $\hat{p}_{2k} = \frac{s_{yk}}{n_{yk}}$ .

The confidence interval is then  $\hat{\delta}_{MH} \pm z_{1-\alpha/2} \sqrt{\hat{\sigma}^2(\hat{d}_{MH})}$ .

## Value

An object containing the following components:

estimate	The Mantel-Haenszel estimated common risk difference
conf.low	Lower bound of the confidence interval
conf.high	Upper bound of the confidence interval
conf.level	The confidence level used
variance	Variance estimate
statistic	Z-Statistic under the null hypothesis, assuming a common risk difference of 0
p.value	p-value under the null hypothesis, assuming a common risk difference of 0
method	Description of the method used ("Mantel-Haenszel Confidence Interval, Sato Variance") or ("Mantel-Haenszel Confidence Interval, Independent Binomial")

## References

Agresti, A. (2013). Categorical Data Analysis. 3rd Edition. John Wiley & Sons, Hoboken, NJ p. 231  
 Cochran, W.G. (1954). The Combination of estimates from different experiments. Biometrics, 10(1), p.101-129

## Examples

```
# Generate binary samples with strata
responses <- expand(c(9, 3, 7, 2), c(10, 10, 10, 10))
arm <- rep(c("treat", "control"), 20)
strata <- rep(c("stratum1", "stratum2"), times = c(20, 20))

# Calculate common risk difference
ci_prop_diff_mh_strata(x = responses, by = arm, strata = strata)
# Calculate risk difference with independent binomial variance
ci_prop_diff_mh_strata(x = responses, by = arm, strata = strata, sato_var = FALSE)
```

---

ci_prop_diff_mn	<i>Miettinen-Nurminen Confidence Interval for Difference in Proportions</i>
-----------------	---

---

### Description

Calculates the Miettinen-Nurminen (MN) confidence interval for the difference between two proportions. This method can be more accurate than traditional methods, especially with small sample sizes or proportions close to 0 or 1.

### Usage

```
ci_prop_diff_mn(x, by, conf.level = 0.95, delta = NULL, data = NULL)
```

### Arguments

x	(binary/numeric/logical) vector of a binary values, i.e. a logical vector, or numeric with values $c(0, 1)$
by	(string) A character or factor vector with exactly two unique levels identifying the two groups to compare. Can also be a column name if a data frame provided in the data argument.
conf.level	(scalar numeric) a scalar in (0,1) indicating the confidence level. Default is 0.95
delta	(numeric) Optionally a single number or a vector of numbers between -1 and 1 (not inclusive) to set the difference between two groups under the null hypothesis. If provided, the function returns the test statistic and p-value under the delta hypothesis.
data	(data.frame) Optional data frame containing the variables specified in x and by.

### Details

The function implements the Miettinen-Nurminen method to compute confidence intervals for the difference between two proportions. This approach:

- Calculates the Miettinen-Nurminen score test statistic for different possible values of the proportion difference (delta)
- Identifies the delta values where the test statistic equals the critical value corresponding to the desired confidence level
- Returns these boundary values as the confidence interval limits

The method uses a score test with a small-sample correction factor, making it more accurate than normal approximation methods, especially for small samples or extreme proportions. The equation for the test statistics is as follows:

$$H_0 : \hat{d} - \delta \leq 0 \quad \text{vs.} \quad H_1 : \hat{d} - \delta > 0$$

$$T_\delta = \frac{\hat{p}_x - \hat{p}_y - \delta}{\sigma_{mn}(\delta)}$$

where  $\hat{p}_* = s_*/n_*$  represent the observed number of successes divided by the number of participant in that group. The  $\sigma_{mn}(\delta)$  is a function of the delta values and is create with the following equation"  $\tilde{p}_*$  represent the MLE of the proportions.

$$\sigma_{mn}(\delta) = \sqrt{\left[ \frac{\tilde{p}_y(1 - \tilde{p}_y)}{n_x} + \frac{\tilde{p}_x(1 - \tilde{p}_x)}{n_y} \right] \left( \frac{N}{N - 1} \right)}$$

$\tilde{p}_x = 2p \cdot \cos(a) - \frac{L_2}{3L_3}$  and  $\tilde{p}_y = \tilde{p}_x + \delta$  where:

- $p = \pm \sqrt{\frac{L_2^2}{(3L_3)^2} - \frac{L_1}{3L_3}}$
- $a = 1/3[\pi + \cos^{-1}(q/p^3)]$
- $q = \frac{L_2^3}{(3L_3)^3} - \frac{L_1L_2}{6L_3^2} + \frac{L_0}{2L_3}$
- $L_3 = n_x + n_y$
- $L_2 = (n_x + 2n_y)\delta - N - (s_x + s_y)$
- $L_1 = (n_y\delta - L_3 - 2s_y)\delta + s_x + s_y$
- $L_0 = s_y\delta(1 - \delta)$

For more information about these equations see Miettinen (1985)

## Value

An object containing the following components:

estimate	The point estimate of the difference in proportions (p_x - p_y)
conf.low	Lower bound of the confidence interval
conf.high	Upper bound of the confidence interval
conf.level	The confidence level used
delta	delta value(s) used
statistic	Z-Statistic under the null hypothesis based on the given 'delta'
p.value	p-value under the null hypothesis based on the given 'delta'
method	Description of the method used ("Miettinen-Nurminen Confidence Interval")

If delta is not provided statistic and p.value will be NULL

## References

Miettinen, O. S., & Nurminen, M. (1985). Comparative analysis of two rates. *Statistics in Medicine*, 4(2), 213-226.

**Examples**

```
# Generate binary samples
responses <- expand(c(9, 3), c(10, 10))
arm <- rep(c("treat", "control"), times = c(10, 10))

# Calculate 95% confidence interval for difference in proportions
ci_prop_diff_mn(x = responses, by = arm)

# Calculate 99% confidence interval
ci_prop_diff_mn(x = responses, by = arm, conf.level = 0.99)

# Calculate the p-value under the null hypothesis delta = -0.1
ci_prop_diff_mn(x = responses, by = arm, delta = -0.1)

# Calculate from a data.frame
data <- data.frame(responses, arm)
ci_prop_diff_mn(x = responses, by = arm, data = data)
```

---

```
ci_prop_diff_mn_strata
```

*Stratified Miettinen-Nurminen Confidence Interval for Difference in Proportions*

---

**Description**

Calculates Stratified Miettinen-Nurminen (MN) confidence intervals and corresponding point estimates for the difference between two proportions

**Usage**

```
ci_prop_diff_mn_strata(
  x,
  by,
  strata,
  method = c("score", "summary score"),
  conf.level = 0.95,
  delta = NULL,
  data = NULL
)
```

**Arguments**

x	(binary/numeric/logical) vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)
by	(string) A character or factor vector with exactly two unique levels identifying the two groups to compare. Can also be a column name if a data frame provided in the data argument.

strata	(numeric) A vector specifying the stratum for each observation. It needs to be the length of x or a multiple of x if multiple levels of strata are present. Can also be a column name (or vector of column names NOT quoted) if a data frame provided in the data argument.
method	(string) Specifying how the CIs should be calculated. It must equal either 'score' or 'summary score'. See details for more information about the implementation differences.
conf.level	(scalar numeric) a scalar in (0,1) indicating the confidence level. Default is 0.95
delta	(numeric) Optionally a single number or a vector of numbers between -1 and 1 (not inclusive) to set the difference between two groups under the null hypothesis. If provided, the function returns the test statistic and p-value under the delta hypothesis.
data	(data.frame) Optional data frame containing the variables specified in x and by.

### Details

The function implements the stratified Miettinen-Nurminen method to compute confidence intervals for the difference between two proportions across multiple strata.

$$H_0 : \hat{d} - \delta \leq 0 \quad \text{vs.} \quad H_1 : \hat{d} - \delta > 0$$

The "score" method is a weighted MN score first described in the original 1985 paper. The formula is:

- Calculates weights for each stratum as  $w_i = \frac{n_{xi} \cdot n_{yi}}{n_{xi} + n_{yi}}$
- Computes the overall weighted difference  $\hat{d} = \frac{\sum w_i \hat{p}_{xi}}{\sum w_i} - \frac{\sum w_i \hat{p}_{yi}}{\sum w_i}$
- Uses the stratified test statistic:

$$Z_\delta = \frac{\hat{d} - \delta}{\sqrt{\sum_{i=1}^k \left( \frac{w_i}{\sum w_i} \right)^2 \cdot \hat{\sigma}_{mn}^2(d)}}$$

- Finds the range of all values of  $\delta$  for which the stratified test statistic ( $Z_\delta$ ) falls in the acceptance region  $\{Z_\delta < z_{\alpha/2}\}$

The  $\hat{\sigma}_{mn}^2(\hat{d})$  is the Miettinen-Nurminen variance estimate. See the details of [ci\\_prop\\_diff\\_mn\(\)](#) for how  $\hat{\sigma}_{mn}^2(\delta)$  is calculated.

The "summary score" method follows the meta-analyses proposed in Agresti 2013 and is consistent with the "Summary Score Confidence Limits" method used in SAS. The formula is:

- The point estimate of the stratified risk difference is a weighted average of the midpoints of the within-stratum MN confidence intervals:

$$\hat{d}_S = \sum_i \hat{d}_i w_i$$

- Define  $s_i$  as the width of the CI for the  $i$ th stratum divided by  $2 \times z_{\alpha/2}$  and then stratum weights are given by

$$w_i = \left( \frac{1}{s_i^2} \right) / \sum_i \left( \frac{1}{s_i^2} \right)$$

- The variance of  $\hat{d}_S$  is computed as

$$\widehat{\text{Var}}(\hat{d}_S) = \frac{1}{\sum_i \left( \frac{1}{s_i^2} \right)}$$

- Confidence limits for the stratified risk difference estimate are

$$\hat{d}_S \pm \left( z_{\alpha/2} \times \widehat{\text{Var}}(\hat{d}_S) \right)$$

## Value

An object containing the following components:

estimate	The point estimate of the difference in proportions (p_x - p_y)
conf.low	Lower bound of the confidence interval
conf.high	Upper bound of the confidence interval
conf.level	The confidence level used
delta	delta value(s) used
statistic	Z-Statistic under the null hypothesis based on the given 'delta'
p.value	p-value under the null hypothesis based on the given 'delta'
method	Description of the method used ("Stratified {method} Miettinen-Nurminen Confidence Interval")

If delta is not provided statistic and p.value will be NULL

## References

Miettinen, O. S., & Nurminen, M. (1985). Comparative analysis of two rates. *Statistics in Medicine*, 4(2), 213-226.

[Common Risk Difference :: Base SAS\(R\) 9.4 Procedures Guide: Statistical Procedures, Third Edition](#)

Agresti, A. (2013). *Categorical Data Analysis*. 3rd Edition. John Wiley & Sons, Hoboken, NJ

## Examples

```
# Generate binary samples with strata
responses <- expand(c(9, 3, 7, 2), c(10, 10, 10, 10))
arm <- rep(c("treat", "control"), 20)
strata <- rep(c("stratum1", "stratum2"), times = c(20, 20))

# Calculate stratified confidence interval for difference in proportions
ci_prop_diff_mn_strata(x = responses, by = arm, strata = strata)
```

```
# Using the summary score method
ci_prop_diff_mn_strata(x = responses, by = arm, strata = strata,
                      method = "summary score")

# Calculate 99% confidence interval
ci_prop_diff_mn_strata(x = responses, by = arm, strata = strata,
                      conf.level = 0.99)

# Calculate p-value under null hypothesis delta = 0.2
ci_prop_diff_mn_strata(x = responses, by = arm, strata = strata,
                      delta = 0.2)
```

---

ci_prop_diff_nc	<i>Newcombe Confidence Interval for Difference in Proportions</i>
-----------------	---

---

## Description

Newcombe Confidence Interval for Difference in Proportions

## Usage

```
ci_prop_diff_nc(x, by, conf.level = 0.95, correct = FALSE, data = NULL)
```

## Arguments

x	(binary/numeric/logical) vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)
by	(string) A character or factor vector with exactly two unique levels identifying the two groups to compare. Can also be a column name if a data frame provided in the data argument.
conf.level	(scalar numeric) a scalar in (0,1) indicating the confidence level. Default is 0.95
correct	(logical) apply continuity correction.
data	(data.frame) Optional data frame containing the variables specified in x and by.

## Details

The **Wilson (Score)** confidence limits without continuity correction for each individual binomial proportion,  $p_i = x_i/n_i$ , for  $i = 1, 2$ , are given by:

$$\frac{(2n_i\hat{p}_i + z^2) \pm z\sqrt{4n_i\hat{p}_i(1 - \hat{p}_i) + z^2}}{2(n_i + z^2)}$$

Denote the lower and upper Wilson (Score) confidence limits for  $p_i$  as  $L_i$  and  $U_i$ , respectively.

Then, the **Newcombe (Score)** confidence limits for the difference in proportions ( $p_1 - p_2$ ) are given by:

$$\text{Lower limit: } (\hat{p}_1 - \hat{p}_2) - \sqrt{(\hat{p}_1 - L_1)^2 + (U_2 - \hat{p}_2)^2}$$

$$\text{Upper limit: } (\hat{p}_1 - \hat{p}_2) + \sqrt{(U_1 - \hat{p}_1)^2 + (\hat{p}_2 - L_2)^2}$$

The confidence intervals with continuity correction for each individual binomial proportion are obtained using the **Wilson (Score) confidence limits with continuity correction**.

For each binomial proportion  $p_i = x_i/n_i$ , where  $i = 1, 2$ , the confidence intervals are given by:

$$\frac{2n_i\hat{p}_i + z^2}{2(n_i + z^2)} \pm \frac{z}{2(n_i + z^2)} \sqrt{z^2 - \frac{2}{n_i} + 4\hat{p}_i[n_i(1 - \hat{p}_i) + 1]}$$

### Value

An object containing the following components:

n	The number of responses for each group
N	The total number in each group
estimate	The point estimate of the difference in proportions
conf.low	Lower bound of the confidence interval
conf.high	Upper bound of the confidence interval
conf.level	The confidence level used
method	Anderson-Hauck Confidence Interval

### References

Newcombe, R. G. (1998). Interval estimation for the difference between independent proportions: Comparison of eleven methods. *Statistics in Medicine*, 17(8), 873–890. [Constructing Confidence Intervals for the Differences of Binomial Proportions in SAS](#)

### Examples

```
responses <- expand(c(9, 3), c(10, 10))
arm <- rep(c("treat", "control"), times = c(10, 10))

# Calculate 95% confidence interval for difference in proportions
ci_prop_diff_nc(x = responses, by = arm)
```

---

ci\_prop\_diff\_nc\_strata

*Stratified Newcombe Common Risk Difference Confidence Interval*


---

### Description

Calculates the stratified Newcombe confidence interval for unequal proportions as described in Yan X, Su XG. Stratified Wilson and Newcombe confidence intervals or multiple binomial proportions. Weights are estimated using CMH or Wilson methods.

### Usage

```
ci_prop_diff_nc_strata(
  x,
  by,
  strata,
  conf.level = 0.95,
  correct = FALSE,
  weights_method = c("wilson", "cmh"),
  data = NULL
)
```

### Arguments

x	(binary/numeric/logical) vector of a binary values, i.e. a logical vector, or numeric with values $c(0, 1)$
by	(string) A character or factor vector with exactly two unique levels identifying the two groups to compare. Can also be a column name if a data frame provided in the data argument.
strata	(numeric) A vector specifying the stratum for each observation. It needs to be the length of x or a multiple of x if multiple levels of strata are present. Can also be a column name (or vector of column names NOT quoted) if a data frame provided in the data argument.
conf.level	(scalar numeric) a scalar in (0,1) indicating the confidence level. Default is 0.95
correct	(scalar logical) include the continuity correction. For further information, see for example [ci_prop_diff_nc()]. [ci_prop_diff_nc()]: R:ci_prop_diff_nc()
weights_method	(character) Can be either "wilson" or "cmh" and directs the way weights are estimated.
data	(data.frame) Optional data frame containing the variables specified in x and by.

**Details**

$$L = \hat{d}_{MH} - z_{\alpha/2} \sqrt{\sum_h w_h^2 L_{2h}(1 - L_{2h}) + \sum_h w_h^2 U_{1h}(1 - U_{1h})}$$

$$U = \hat{d}_{MH} + z_{\alpha/2} \sqrt{\sum_h w_h^2 L_{2h}(1 - L_{2h}) + \sum_h w_h^2 U_{1h}(1 - U_{1h})}$$

Where:

- $\hat{d}_{MH}$ : Mantel-Haenszel common risk difference
- $z_{\alpha/2}$ : standard normal critical value
- $w_h$ : stratum weights
- $L_{2h}, U_{1h}$ : Wilson-type CI limits for stratum h

**Value**

An object containing the following components:

n	Number of responses
N	Total number
estimate	The point estimate of the proportion
conf.low	Lower bound of the confidence interval
conf.high	Upper bound of the confidence interval
conf.level	The confidence level used
weights	Weights of each strata calculated as per the specified "weights_method" argument.
method	Type of method used

**Examples**

```
set.seed(1)
rsp <- sample(c(TRUE, FALSE), 100, TRUE)
grp <- sample(c("Placebo", "Treatment"), 100, TRUE)
strata_data <- data.frame(
  "f1" = sample(c("a", "b"), 100, TRUE),
  "f2" = sample(c("x", "y", "z"), 100, TRUE),
  stringsAsFactors = TRUE
)
strata <- interaction(strata_data)

ci_prop_diff_nc_strata(
  x = rsp, by = grp, strata = strata, weights_method = "cmh",
  conf.level = 0.95
)
```

---

ci_prop_diff_wald	<i>Wald Confidence Interval for Difference in Proportions</i>
-------------------	---

---

**Description**

Calculates the Wald interval by following the usual textbook definition for a difference in proportions confidence interval using the normal approximation.

**Usage**

```
ci_prop_diff_wald(x, by, conf.level = 0.95, correct = FALSE, data = NULL)
```

**Arguments**

x	(binary/numeric/logical) vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)
by	(string) A character or factor vector with exactly two unique levels identifying the two groups to compare. Can also be a column name if a data frame provided in the data argument.
conf.level	(scalar numeric) a scalar in (0,1) indicating the confidence level. Default is 0.95
correct	(logical) apply continuity correction.
data	(data.frame) Optional data frame containing the variables specified in x and by.

**Details**

$$(\hat{p}_1 - \hat{p}_2) \pm z_{\alpha/2} \sqrt{\frac{\hat{p}_1(1 - \hat{p}_1)}{n_1} + \frac{\hat{p}_2(1 - \hat{p}_2)}{n_2}}$$

**Value**

An object containing the following components:

n	Number of responses in each by group
N	Total number in each by group
estimate	The point estimate of the difference in proportions (p_1 - p_2)
conf.low	Lower bound of the confidence interval
conf.high	Upper bound of the confidence interval
conf.level	The confidence level used
method	Type of method used

**Examples**

```

responses <- expand(c(9, 3), c(10, 10))
arm <- rep(c("treat", "control"), times = c(10, 10))

# Calculate 95% confidence interval for difference in proportions
ci_prop_diff_wald(x = responses, by = arm)

```

---

ci\_prop\_jeffreys      *Jeffreys CI*

---

**Description**

Calculates the Jeffreys interval, an equal-tailed interval based on the non-informative Jeffreys prior for a binomial proportion.

**Usage**

```
ci_prop_jeffreys(x, conf.level = 0.95, data = NULL)
```

**Arguments**

x	(binary/numeric/logical) vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)
conf.level	(scalar numeric) a scalar in (0,1) indicating the confidence level. Default is 0.95
data	(data.frame) Optional data frame containing the variables specified in x and by.

**Details**

$$\left( \text{Beta} \left( \frac{k}{2} + \frac{1}{2}, \frac{n-k}{2} + \frac{1}{2} \right)_{\alpha}, \text{Beta} \left( \frac{k}{2} + \frac{1}{2}, \frac{n-k}{2} + \frac{1}{2} \right)_{1-\alpha} \right)$$

**Value**

An object containing the following components:

n	Number of responses
N	Total number
estimate	The point estimate of the proportion
conf.low	Lower bound of the confidence interval
conf.high	Upper bound of the confidence interval
conf.level	The confidence level used
method	Type of method used

ci\_prop\_mid\_p

*Mid-P CI***Description**

Calculates the exact mid-p CI for binomial proportions by inverting two one-sided binomial tests that include the mid-p tail. This is calculated by finding the  $P_L$  and  $P_U$  that satisfies the following equations:

$$\sum_{x=n_1+1}^n \binom{n}{x} P_L^x (1 - P_L)^{n-x} + \frac{1}{2} \binom{n}{n_1} P_L^{n_1} (1 - P_L)^{n-n_1} = \alpha/2$$

$$\sum_{x=0}^{n_1-1} \binom{n}{x} P_U^x (1 - P_U)^{n-x} + \frac{1}{2} \binom{n}{n_1} P_U^{n_1} (1 - P_U)^{n-n_1} = \alpha/2$$

**Usage**

```
ci_prop_mid_p(x, conf.level = 0.95, data = NULL)
```

**Arguments**

**x** (binary/numeric/logical)  
vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)

**conf.level** (scalar numeric)  
a scalar in (0,1) indicating the confidence level. Default is 0.95

**data** (data.frame)  
Optional data frame containing the variables specified in x and by.

**Value**

An object containing the following components:

**n** Number of responses

**N** Total number

**estimate** The point estimate of the proportion

**conf.low** Lower bound of the confidence interval

**conf.high** Upper bound of the confidence interval

**conf.level** The confidence level used

**method** Type of method used

---

 ci\_prop\_wald

 Wald CI
 

---

### Description

Calculates the Wald interval by following the usual textbook definition for a single proportion confidence interval using the normal approximation.

### Usage

```
ci_prop_wald(x, conf.level = 0.95, correct = FALSE, data = NULL)
```

### Arguments

x	(binary/numeric/logical) vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)
conf.level	(scalar numeric) a scalar in (0,1) indicating the confidence level. Default is 0.95
correct	(logical) apply continuity correction.
data	(data.frame) Optional data frame containing the variables specified in x and by.

### Details

$$\hat{p} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}(1 - \hat{p})}{n}}$$

### Value

An object containing the following components:

n	Number of responses
N	Total number
estimate	The point estimate of the proportion
conf.low	Lower bound of the confidence interval
conf.high	Upper bound of the confidence interval
conf.level	The confidence level used
method	Type of method used

**Examples**

```
# example code
x <- c(
  TRUE, TRUE, TRUE, TRUE, TRUE,
  FALSE, FALSE, FALSE, FALSE, FALSE
)

ci_prop_wald(x, conf.level = 0.9)
```

---

ci_prop_wilson	<i>Wilson CI</i>
----------------	------------------

---

**Description**

Calculates the Wilson interval by calling `stats::prop.test()`. Also referred to as Wilson score interval.

**Usage**

```
ci_prop_wilson(x, conf.level = 0.95, correct = FALSE, data = NULL)
```

**Arguments**

x	(binary/numeric/logical) vector of a binary values, i.e. a logical vector, or numeric with values $c(0, 1)$
conf.level	(scalar numeric) a scalar in (0,1) indicating the confidence level. Default is 0.95
correct	(logical) apply continuity correction.
data	(data.frame) Optional data frame containing the variables specified in x and by.

**Details**

$$\frac{\hat{p} + \frac{z_{\alpha/2}^2}{2n} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}(1-\hat{p})}{n} + \frac{z_{\alpha/2}^2}{4n^2}}}{1 + \frac{z_{\alpha/2}^2}{n}}$$

**Value**

An object containing the following components:

n	Number of responses
N	Total number
estimate	The point estimate of the proportion

conf.low	Lower bound of the confidence interval
conf.high	Upper bound of the confidence interval
conf.level	The confidence level used
method	Type of method used

---

ci\_prop\_wilson\_strata *Stratified Wilson CI*

---

### Description

Calculates the stratified Wilson confidence interval for unequal proportions as described in Xin YA, Su XG. Stratified Wilson and Newcombe confidence intervals for multiple binomial proportions. *Statistics in Biopharmaceutical Research*. 2010;2(3).

### Usage

```
ci_prop_wilson_strata(
  x,
  strata,
  weights = NULL,
  conf.level = 0.95,
  max.iterations = 10L,
  correct = FALSE,
  data = NULL
)
```

### Arguments

x	(binary/numeric/logical) vector of a binary values, i.e. a logical vector, or numeric with values $c(0, 1)$
strata	(numeric) A vector specifying the stratum for each observation. It needs to be the length of x or a multiple of x if multiple levels of strata are present. Can also be a column name (or vector of column names NOT quoted) if a data frame provided in the data argument.
weights	(numeric) weights for each level of the strata. If NULL, they are estimated using the iterative algorithm that minimizes the weighted squared length of the confidence interval.
conf.level	(scalar numeric) a scalar in (0,1) indicating the confidence level. Default is 0.95
max.iterations	(positive integer) maximum number of iterations for the iterative procedure used to find estimates of optimal weights.

correct	(scalar logical) include the continuity correction. For further information, see for example <code>stats::prop.test()</code> .
data	(data.frame) Optional data frame containing the variables specified in <code>x</code> and <code>by</code> .

### Details

$$\frac{\hat{p}_j + \frac{z_{\alpha/2}^2}{2n_j} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}_j(1-\hat{p}_j)}{n_j} + \frac{z_{\alpha/2}^2}{4n_j^2}}}{1 + \frac{z_{\alpha/2}^2}{n_j}}$$

### Value

An object containing the following components:

n	Number of responses
N	Total number
estimate	The point estimate of the proportion
conf.low	Lower bound of the confidence interval
conf.high	Upper bound of the confidence interval
conf.level	The confidence level used
weights	Weights of each strata, will be the same as the input unless unspecified, then it will be the dynamically calculated weights.
method	Type of method used

### Examples

```
# Stratified Wilson confidence interval with unequal probabilities

set.seed(1)
rsp <- sample(c(TRUE, FALSE), 100, TRUE)
strata_data <- data.frame(
  "f1" = sample(c("a", "b"), 100, TRUE),
  "f2" = sample(c("x", "y", "z"), 100, TRUE),
  stringsAsFactors = TRUE
)
strata <- interaction(strata_data)
n_strata <- ncol(table(rsp, strata)) # Number of strata

ci_prop_wilson_strata(
  x = rsp, strata = strata,
  conf.level = 0.90
)

# Not automatic setting of weights
ci_prop_wilson_strata(
```

```

x = rsp, strata = strata,
weights = rep(1 / n_strata, n_strata),
conf.level = 0.90
)

```

---

ci\_rel\_risk\_cmh\_strata

*Mantel-Haenszel Stratified Relative Risk Confidence Interval*

---

### Description

Calculates the confidence interval for the Mantel-Haenszel estimate of the common relative risk across multiple 2x2 tables (strata)

### Usage

```
ci_rel_risk_cmh_strata(x, by, strata, conf.level = 0.95, data = NULL)
```

### Arguments

x	(binary/numeric/logical) vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)
by	(string) A character or factor vector with exactly two unique levels identifying the two groups to compare. Can also be a column name if a data frame provided in the data argument.
strata	(numeric) A vector specifying the stratum for each observation. It needs to be the length of x or a multiple of x if multiple levels of strata are present. Can also be a column name (or vector of column names NOT quoted) if a data frame provided in the data argument.
conf.level	(scalar numeric) a scalar in (0,1) indicating the confidence level. Default is 0.95
data	(data.frame) Optional data frame containing the variables specified in x and by.

### Details

The Mantel-Haenszel relative risk difference is computed as:

$$RR_{MH} = \frac{\sum_k s_{xk} n_{yk} / N_k}{\sum_k s_{yk} n_{xk} / N_k}$$

The variance is:

$$\hat{\sigma}^2 = \widehat{Var}(\log(RR_{MH})) = \frac{\sum_k (n_{xk} n_{yk} (s_{xk} + s_{yk}) - s_{xk} s_{yk} N_k) / N_k^2}{(\sum_k s_{xk} n_{yk} / N_k)(\sum_k s_{yk} n_{xk} / N_k)}$$

The confidence interval is then  $(RR_{MH} \times \exp(-z_{1-\alpha/2}\sqrt{\hat{\sigma}^2}), RR_{MH} \times \exp(z_{1-\alpha/2}\sqrt{\hat{\sigma}^2}))$ .

### Value

An object containing the following components:

estimate	The Mantel-Haenszel estimated common risk difference
conf.low	Lower bound of the confidence interval
conf.high	Upper bound of the confidence interval
conf.level	The confidence level used
variance	Mantel-Haenszel variance estimate $Var(\log(RR_{MH}))$
method	Description of the method used ("Mantel-Haenszel Common Relative Risk Confidence Interval")

### References

Agresti, A. (2013). *Categorical Data Analysis*. 3rd Edition. John Wiley & Sons, Hoboken, NJ

### Examples

```
# Generate binary samples with strata
responses <- expand(c(9, 3, 7, 2), c(10, 10, 10, 10))
arm <- rep(c("treat", "control"), 20)
strata <- rep(c("stratum1", "stratum2"), times = c(20, 20))

# Calculate common risk difference
ci_rel_risk_cmh_strata(x = responses, by = arm, strata = strata)
```

---

expand

*Expand Count Data into Binary Vectors*

---

### Description

Converts count data (number of successes and total sample size) into a binary vector of TRUE/FALSE values. This is useful for converting summary statistics back into raw data format for analysis functions that require individual-level data.

### Usage

```
expand(x, n)
```

**Arguments**

x	Integer (or vector of integers) representing the number of successes.
n	Integer (or vector of integers) representing the total number of participants.

**Details**

For each pair of values in x and n, the function creates a vector with x TRUE values followed by n-x FALSE values. If multiple pairs are provided, the resulting vectors are concatenated in order.

**Value**

A logical vector where TRUE represents a success and FALSE represents a failure. The length of the vector equals the sum of all sample sizes.

**Examples**

```
# Convert 4 successes out of 13 participants to binary data
expand(4, 13)

# Convert multiple groups of data
# Group 1: 9 successes out of 10
# Group 2: 3 successes out of 10
expand(c(9, 3), c(10, 10))
```

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